MATH 361: Statistical Methods I (4-0-4) 10-05-2017

Catalog Description: Graphical representation of statistical data, measures of central tendency and variability, and elementary probability. Applications of binomial, normal, t, F, and chi-square distributions; tests of hypothesis; regression and correlation analysis. Multiple regression, analysis of variance and design and analysis of experiments.

Course Objectives: After completing this course, students will be able to

- 1. Describe patterns and departures from patterns in data.
- 2. Use probability rules and distributions, including the binomial and normal distributions, to solve problems.
- 3. Perform statistical inference.

Learning Outcomes and Performance Criteria

1. Organize and describe data with numerical measures.

Core Criteria:

- (a) Calculate the mean.
- (b) Compare and contrast two data sets in terms of their means, variances, and standard deviations.
- (c) Calculate the five number summary.
- (d) Answer questions about a data set based on the five number summary.
- (e) Calculate the linear correlation coefficient.
- (f) Calculate the least squares regression line.
- (g) Compare and contrast the correlation coefficient for two data sets (strength and direction).
- (h) Interpret the slope of a least squares regression line in terms of the variables.
- (i) Interpret the coefficient of determination as the percentage of variation in the response variable explained by the linear model.

Additional Criteria:

- (a) Calculate the coefficient of determination.
- (b) Calculate the mode.
- (c) Interpret the y-intercept of a least squares regression line.
- 2. Organize and describe data graphically.

Core Criteria:

- (a) Create and interpret a box-plot.
- (b) Create and interpret a histogram.
- (c) Create and interpret a scatter-plot.

(d) Compare multiple graphs for different data sets.

Additional Criteria:

- (a) Create and interpret a dot-plot.
- (b) Create and interpret a steam and leaf diagram.
- (c) Create and interpret a pie chart.
- (d) Create and interpret a cumulative frequency plot.
- 3. Describe data with appropriate vocabulary.

Core Criteria:

- (a) Determine if data is qualitative or quantitative.
- (b) Determine if data is discrete or continuous.
- (c) Distinguish between the explanatory and response variables.
- (d) Determine if data is skewed or symmetric.
- 4. Calculate and interpret probabilities with discrete distributions using one or more of the following:

Core Criteria:

- (a) Addition rule.
- (b) Multiplication rule.
- (c) Conditional probability.
- (d) Marginal probability.
- (e) Independent events.
- (f) Dependent events
- (g) Compliment.
- (h) Combination.
- (i) Permutation.
- (j) Multiplication law.
- (k) Binomial distribution.
- (l) Mean and standard deviation of the binomial distribution.
- (m) Tree diagram.
- (n) Expected Value

Additional Criteria:

- (a) Probability distribution.
- (b) Law of large numbers.
- (c) Standard deviation of a probability distribution.

5. Calculate and interpret probabilities with continuous distributions using one or more of the following distributions or concepts:

Core Criteria:

- (a) Normal Distribution.
- (b) Sampling Distribution of the mean.
- (c) Central limit theorem.
- (d) T-Distribution.

Additional Criteria:

- (a) Proportions.
- 6. Make inferences about population mean(s) using a confidence interval:

Core Criteria:

- (a) Compute confidence intervals for the mean of a large sample (z-value).
- (b) Compute confidence intervals for the mean of a small sample (t-value).
- (c) Compute confidence intervals for the difference of two means. (dependant and independent)
- (d) Interpret a confidence interval.

Additional Criteria:

- (a) Compute confidence intervals for the mean for a proportion.
- (b) Test hypothesis for one or two proportion(s).
- 7. Make inferences about population mean(s) by hypothesis testing:

Core Criteria:

- (a) Test hypothesis for one or two mean(s).
- (b) Conduct a one-sample, two-sample or paired t-test:
 - Write the null and alternative hypotheses.
 - Determine the test statistic t and the degrees of freedom df.
 - Determine the *P*-value using technology or give an appropriate interval that includes the *P*-value.
 - Decide whether or not to reject the null hypothesis and write a conclusion.
- (c) Determine whether a t-test is one or two-tailed.
- (d) Determine when a paired t-test should be used.
- (e) Quantitative evidence from a hypothesis test is conveyed, and explained in such a way that a competent non-expert reader can follow along.